A New Optimal Voltage Control Technique For UPS System

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Abstract- This paper proposes a simple best possible voltage control technique for three-stage uninterruptible-control supply frameworks. The proposed voltage controller is made out of an input control term and a repaying control term. The previous term is intended to make the framework errors focalize to zero, while the last term is connected to make up for the framework vulnerabilities. In addition, the ideal load current observer is utilized to enhance cost of the system and reliability. Especially, the closed loop security of a observer based ideal voltage control law is scientifically demonstrated by demonstrating that the entire conditions of the enlarged observer based control framework errors exponentially join to zero. Dissimilar to past algorithm, the proposed strategy can make a tradeoff between control input extent and following error by just picking appropriate performance indexes. The viability of the proposed controller is approved through recreations on MATLAB/Simulink. Finally, the relative outcomes for the proposed conspire and the customary input linearization control plot and a fuzzy logic controller are exhibited to show that the proposed calculation accomplishes a great execution, for example, quick transient reaction, little enduring state error, and low aggregate harmonic distortion under load step change, uneven load, and nonlinear load with the parameter variations.

Index Terms— Optimal load current observer, optimal voltage control, three-phase inverter, total harmonic distortion (THD), uninterruptible power supply (UPS).

INTRODUCTION

UNINTERRUPTIBLE power supply (UPS) systems supply emergency power in case of utility power failures. Recently, the importance of the UPS systems has been intensified more and more due to the increase of sensitive and critical applications such as communication systems, medical equipment, semiconductor manufacturing systems, and data processing systems [1]–[3]. These applications require clean power and high reliability regardless of the electric power failures and distorted utility supply voltage. Thus, the performance of the UPS systems is usually evaluated in terms of the total harmonic distortion (THD) of the output voltage and the transient/steady state responses regardless of the load conditions: load step change, linear load, and nonlinear load [4]–[7]. To improve the aforementioned performance indexes, a number of control algorithms have been proposed such as proportional–integral (PI) control, $H_\infty$ loop-shaping control, model predictive control, deadbeat control, sliding-mode control, repetitive control, adaptive control, and feedback linearization control (FLC). The conventional PI control suggested in [8] and [9] is easy to implement; however, the THD value of the output voltage is not low under a nonlinear-load condition,[10], $H_\infty$ loop-shaping control scheme is described and implemented on a single-phase inverter, which has a simple structure and is robust against model uncertainties. A model predictive control method for UPS applications is described in [11]. By using a load current observer in place of current sensors, the authors claimed a reduced system cost. However, the simulation and experimental results do not reveal an exceptional performance in terms of THD and steady-state error. In [12], the deadbeat control method uses the state feedback information to compensate for the voltage drop across the inductor. However, this method exhibits sensitivity to parameter mismatches, and the harmonics of the inverter output voltage are not very well compensated. In [13] and [14], the sliding-mode control technique reflects robustness to the system noise, and still, the control system has a well-known chattering problem. In [15], repetitive control is applied to achieve a high-quality sinusoidal output voltage of a three-phase UPS system. Generally, the control technique has a slow response time. In [16], the adaptive control method with low THD is proposed; nevertheless, there is still a risk of divergence if the controller gains are not properly selected. Multivariable FLC is presented in [17]. In this control technique, the nonlinearity of the system is considered to achieve low THD under nonlinear load. However, it is not easy to carry, out due to the computation complexities. As a result, the aforementioned linear controllers are simple, but the performance is not satisfactory under nonlinear load. In contrast, the nonlinear controllers have an outstanding...
performance, but the implementation is not easy due to the relatively complicated controllers. So far, the optimal control theory has been researched in various fields such as aerospace, economics, physics, and so on [18], since it has a computable solution called a performance index that can quantitatively evaluate the system performance by contrast with other control theories. In addition, the optimal control design gives the optimality of the controller according to a quadratic performance criterion and enables the control system to have good properties such as enough gain and phase margin, robustness to uncertainties, good tolerance of nonlinearities, etc. [19]. Hence, a linear optimal controller has not only a simple structure in comparison with other controllers but also a remarkable control performance similar to other nonlinear controllers [20]–[22].

Therefore, this paper proposes an observer-based optimal voltage control scheme for three-phase UPS systems. This proposed voltage controller encapsulates two main parts: a feedback control term and a compensating control term. The former term is designed to make the system errors converge to zero, and the latter term is applied to estimate the system uncertainties. The Lyapunov theorem is used to analyze the stability of the system. Specially, this paper proves that the closed loop stability of the observer-based optimal voltage control law by showing that the system errors exponentially converge to zero. Moreover, the proposed control scheme can be systematically designed taking into consideration a tradeoff between control input magnitude and tracking error unlike previous algorithms [23].

The efficacy of the proposed control method is verified via simulations on MATLAB/Simulink. In this paper, a conventional FLC method in [17] and a fuzzy controller is selected to demonstrate the comparative results because it has a good performance under a nonlinear-load condition, and its circuit model of a three-phase inverter in [17] is similar to our system model. Finally, the results clearly show that the proposed scheme has a good voltage regulation capability such as fast transient behavior, small steady-state error, and low THD under various load conditions such as load step change, unbalanced load, and nonlinear load in the existence of the parameter variations.

![Fig 1. Three-phase inverter with an LC filter for a UPS system.](image)

**II. SYSTEM DESCRIPTION AND PROBLEM FORMULATION**

The three-phase UPS system with an LC filter is shown in Fig. 1, which is composed of a dc-link voltage ($V_{dc}$), a three phase pulse width modulation (PWM) inverter ($S_1$ ~ $S_6$), an output LC filter ($L_f, C_f$), and a three-phase load (e.g., linear or nonlinear load). Based on Fig. 1, the dynamic model of a three-phase inverter can be derived in a $d-q$ synchronous reference frame as follows [24]:

$$
\begin{align*}
\dot{i}_d &= \omega v_{Ld} + k_2i_d - k_2v_{Ld} \\
\dot{i}_q &= -\omega v_{Lq} + k_2i_q - k_2v_{Lq} \\
\dot{v}_{Ld} &= \omega v_{Lq} - k_1i_d \\
\dot{v}_{Lq} &= -\omega v_{Ld} + k_1i_q
\end{align*}
$$

where $k_1 = 1/C_f$ and $k_2 = 1/L_f$. In system model (1), $v_{Ld}$, $v_{Lq}$, $i_{id}$, and $i_{iq}$ are the state variables, and $vid$ and $viq$ are the control inputs. In this scheme, the assumption is made to construct the optimal voltage controller and optimal load current observer as:

1. The load currents ($i_{Ld}$ and $i_{Lq}$) are unknown and vary very slowly during the sampling period [11].

**III. PROPOSED OPTIMAL VOLTAGE CONTROLLER DESIGN AND STABILITY ANALYSIS**

Here, a simple optimal voltage controller is proposed for system (1). First, let us define the $d-q$-axis inverter current references ($i^*_{id}, i^*_{iq}$) as

$$
i^*_{id} = i_{Ld} - \frac{1}{k_1} v^*_{Lq}, \quad i^*_{iq} = i_{Lq} + \frac{1}{k_1} v^*_{Ld}
$$

Then, the error values of the load voltages and inverter currents are set as
Therefore, system model (1) can be transformed into the following error dynamics:

\[ dq = -vLd * + \frac{1}{k2} \omega_i Lq, \quad i_{dq} = -vLq * + \frac{1}{k2} \omega_i Ld. \] (3)

Note that \( u_d \) is applied to compensate for the system uncertainties as a compensating term. Consider the following Riccati equation for the solution matrix \( P \) [25]:

\[ PA + A^T P - PBR^{-1}B^T P + Q = 0 \] (5)

\( dq = -vLd * + (1/k2)\omega_i Lq, \) and \( dq = -vLq * + (1/k2)\omega_i Ld. \) Note that \( u_d \) is applied to compensate for the system uncertainties as a compensating term. Consider the following Riccati equation for the solution matrix \( P \) [25]: where \( Q \) and \( R \) are the positive definite weighting matrices with sufficient dimensions.

**Remark 1:** Recall that \( Q \) and \( R \) are the weighting matrices [26]. Excessive large error or control input values can be penalized by using properly chosen \( Q \) and \( R \). Generally, the large \( Q \) means a high control performance, whereas the large \( R \) means a small input magnitude. Consequently, there is a tradeoff between \( Q \) and \( R \) in the control system. The \( Q \) and \( R \) parameters generally need to be tuned until satisfactory control results are obtained. Let the diagonal matrices \( Q \) and \( R \) be defined as

\[ Q = \begin{bmatrix} Q_1 & 0 & \ldots & 0 \\ 0 & Q_2 & \ldots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & \ldots & \ldots & Q_m \end{bmatrix}, \quad R = \begin{bmatrix} R_1 & 0 & \ldots & 0 \\ 0 & R_2 & \ldots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & \ldots & \ldots & R_k \end{bmatrix} \]

where \( Q_i \) and \( R_i \) have positive diagonal entries such that \( \sqrt{Q_i} = 1/y_i \text{max} \), where \( i = 1, 2, \ldots, m \), and \( \sqrt{R_i} = 1/u_i \text{max} \). The number \( y_i \text{max} \) is the maximally acceptable deviation value for the \( i \)-th component of output \( y \). The other quantity \( u_i \text{max} \) is the \( i \)-th component of input \( u \).

With an initial guessed value, the diagonal entries of \( Q \) and \( R \) can be adjusted through a trial-and-error method. Then, the optimal voltage controller can be designed by the following equation:

\[ u = -u_d + Kx \] (6)

where \( K = -R^{-1}BTP \) denotes the gain matrix, and \( u_d \) and \( Kx \) represent a feedforward control term and a feedback control term, respectively.

**Remark 2:** The proposed voltage controller, in essence, is designed based on the well-known linear quadratic regulator minimizing the following performance index [27]:

\[ J = \int_0^\infty (x^T Q x + u_n^T R u_n) \, dt \] (7)

where \( x \) is the error, \( u_n = u + u_d \), and \( Q \) and \( R \) are symmetrical positive definite matrices as mentioned above.

![Fig2: Block diagram of the optimal voltage control scheme](image)

**B. Stability Analysis of Voltage Controller**

Consider the following Lyapunov function:

\[ V(x) = x^T P x. \] (8)

From (4)–(6), and (8), the time derivative of \( V(x) \) is given by the following:
This implies that \( x \) exponentially converges to zero.

**Remark 3:** By considering the parameter variations, the state-dependent coefficient matrix \( A \) is rewritten as \( A = A + \Delta A \), where \( \Delta A \) means the value of system parameter variations. Thus, (4) can be transformed into the following error dynamics:

\[
\dot{x} = Ax + B(u + u_d) .
\]

(10)

The new time derivative of (8) is given by the following:

\[
\dot{V}(x) = 2x^T P \dot{x} = x^T (PA + \Delta A + \Delta A^T P + A^T P - 2PBR^{-1}B^T P)x < 0 .
\]

(11)

By (5), (11) is reduced to

\[
\dot{V}(x) = x^T (PA + \Delta A + \Delta A^T P - Q - PBR^{-1}B^T P)x .
\]

(12)

If the following inequality holds for the given \( A \):

\[
P \Delta A + \Delta A^T P < PBR^{-1}B^T P + Q
\]

(13)

then \( V < 0 \) for all nonzero \( x \). Therefore, the proposed optimal voltage control system can tolerate any parameter variation satisfying (13).

**IV. OPTIMAL LOAD CURRENT OBSERVER DESIGN AND STABILITY ANALYSIS**

**A. Optimal Load Current Observer Design**

As seen in (2) and (4), the inverter current references \( (i^*d \text{ and } i^*q) \) and feedforward control term \( (ud) \) need load current information as inputs. To avoid using current sensors, a linear optimal load current observer is introduced in this algorithm. From (1) and the assumption, the following dynamic model is obtained to estimate the load current:

\[
\begin{align*}
\dot{x}_o &= A_o x_o + B_o u_o \\
y &= C_o x_o
\end{align*}
\]

(14)

where \( x_o = [i_{Ld} i_{Lq} v_{Ld} v_{Lq}]^T, u_o = [k_{iLd} k_{iLq}]^T, \)

\[
A_o = \begin{bmatrix}
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
-k_1 & 0 & 0 & \omega \\
0 & -k_1 & -\omega & 0
\end{bmatrix} , B_o = C_o = \begin{bmatrix}
0 & 0 \\
0 & 1 \\
1 & 0
\end{bmatrix}.
\]

Then, the load current observer is expressed as

\[
\dot{x}_o = A_o x_o + B_o u_o - L(y - C_o \hat{x}_o)
\]

(15)

where \( x' = 0 \) and \( i^*d \text{ and } i^*q \) are estimates of \( i_Ld \text{ and } i_Lq \), respectively. In addition, \( L \) is an observer gain matrix calculated by

\[
L = -P_o C_o^T R_o^{-1}
\]

(16)

and \( P_o \) is the solution of the following Riccati equation:

\[
A_o P_o + P_o A_o^T - P_o C_o^T R_o^{-1} C_o P_o + Q_o = 0
\]

(17)

where \( Q_o \) and \( R_o \) are the positive definite weighting matrices with sufficient dimensions. The manner of choosing \( Q_o \) and \( R_o \) is the same as in Remark 1.

**Remark 4:** The fourth-order Kalman–Bucy optimal observer [19] is used to minimize the performance index \( E(xTe x_e) \), where \( x_e = x^{o} - x' \), representing the estimation values of \( xTe x_e \) for the following perturbed model:

\[
\dot{x}_e = (A - LC)x_e + d , y = C x_e + v
\]

(18)

where \( d \in R4 \) and \( v \in R2 \) are independent white Gaussian noise signals with \( E(d) = 0, E(v) = 0, E(dd^T) = Q_o, \) and \( E(vv^T) = R_o \).

**B. Stability Analysis of Load Current Observer**

The error dynamics of the load current observer can be obtained as follows:

\[
\dot{x}_e = (A - LC)x_e .
\]

(19)

Define the Lyapunov function as where \( X = P - I \). Its time derivative along the error dynamics (19) is represented by the following:
This implies that $x_e$ exponentially converges to zero.

V. OBSERVER-BASED CONTROL LAW AND CLOSED-LOOP STABILITY ANALYSIS

A. Observer-Based Control Law

With the estimated load currents achieved from the observer instead of the measured quantities, the inverter current errors and feed forward control term can be obtained as follows:

$$\begin{align*}
\dot{\hat{i}}_{de} &= \hat{i}_{de} - \hat{i}_{Ld} + \frac{1}{k_1} \omega v_{Lq}^*, \\
\dot{\hat{i}}_{qe} &= \hat{i}_{qe} - \hat{i}_{Lq} - \frac{1}{k_1} \omega v_{Ld}^*, \\
\hat{d}_d &= -v_{Ld}^* + \frac{1}{k_2} \dot{\omega} v_{Lq}, \\
\hat{d}_q &= -v_{Lq}^* - \frac{1}{k_2} \dot{\omega} v_{Ld}.
\end{align*}$$

Then, (22) can be rewritten as the following equations:

$$\begin{align*}
\dot{i}_{de} &= i_{de} + [1 \ 0 \ 0 \ 0] x_e, \\
\dot{i}_{qe} &= i_{qe} + [0 \ 1 \ 0 \ 0] x_e, \\
\dot{d}_d &= d_d + \frac{\omega}{k_2} [0 \ 1 \ 0 \ 0] x_e, \\
\dot{d}_q &= d_q - \frac{\omega}{k_2} [1 \ 0 \ 0 \ 0] x_e.
\end{align*}$$

From (6) and (23), the proposed observer-based control law can be achieved as

$$u = -\bar{u}_d + K \bar{x}$$

where $\bar{x} = [v_{de} \ v_{qe} \ \hat{i}_{de} \ \hat{i}_{qe}]^T$, and $\bar{u}_d = [\hat{d}_d \ \hat{d}_q]^T$.

B. Closed-Loop Stability Analysis

For the purpose of analyzing the stability, (24) is rewritten as the following:

$$u = -u_d + K x + H x_e$$

where $H = (\omega / k_2) E + K F, \bar{x} = x + F x_e, E = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{bmatrix}$, and $F = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$.

Let us define the Lyapunov equation as

$$V(x, x_e) = x^T P x + \zeta x_e^T P_0^{-1} x_e$$

where $\zeta$ is a scalar quantity that satisfies the following inequality

$$\zeta > \frac{\|PBH\|^2}{[\lambda_{\min}(Q) \cdot \lambda_{\min}(P_0^{-1}Q_0P_0^{-1})]}.$$
This implies that $x$ and $xe$ exponentially go to zero. As a result, the design procedure of the proposed observer based control law can be summarized as follows.

Step 1) Build system model (1) in the $d - q$ coordinate frame and then derive error dynamics (4) by using system parameters.

Step 2) Set the optimal voltage controller (6) with the feed forward control term ($u_d$) and feedback control term ($K_x$).

Step 3) Define the load current estimation model (14) and build the load current observer (15) by using the Kalman–Bucy optimal observer.

Step 4) Select the observer weighting matrices $Q_o$ and $R_o$ in Riccati equation by referring to Remark 1. Then, choose the observer gain $L$ in (16) using $Q_o$ and $R_o$.

Fuzzy set involves from a participation capacity which could be characterizes by parameters. The incentive in the vicinity of 0 and 1 uncovers a level of enrollment to the fuzzy set. The way toward changing over the fresh contribution to a fuzzy esteem is called as “fuzzificaton.” The yield of the Fuzzier module is interfaced with the standards. The essential operation of FLC is built from fuzzy control rules using the estimations of fuzzy sets as a rule for the mistake and the change of blunder and control activity. Essential fuzzy module is appeared in fig.6.

The outcomes are joined to give a fresh yield controlling the yield variable and this procedure is called as "DEFUZZIFICATION."

Fuzzy rules:
In the fuzzy control, input and output variables are the size of the form to describe in words, so to select special vocabulary to describe these variables, generally used in "big, medium and small" Three words to express the controller input and output variables state, plus the positive and negative directions, and zero, a total of seven words : { negative big, negative medium, negative small, zero, positive small, middle, CT } , the general terms used in the English abbreviation prefix : {NB, NM, NS, ZE, PS, PM, PB}.
VII. SIMULINK MODELLING AND RESULTS

The proposed voltage control algorithm is carried out in various conditions (i.e., load step change, unbalanced load, and nonlinear load) to impeccably expose its merits. In order to instantly engage and disengage the load during a transient condition, the on–off switch is employed as shown in Fig. 3. The resistive load depicted in Fig. 4(a) is applied under both the load step change condition (i.e., 0%–100%) and the unbalanced load condition (i.e., phase B opened) to test the robustness of the proposed scheme when the load is suddenly disconnected. In practical applications, the most common tolerance variations of the filter inductance \( L_f \) and filter capacitance \( C_f \), which are used as an output filter, are within \( \pm 10\% \). To further justify the robustness under parameter variations, a 30% reduction in both \( L_f \) and \( C_f \) is assumed under all load conditions such as load step change, unbalanced load, and nonlinear load. Fig. 7 shows the simulation results of the proposed control method during the load step change. Moreover, Fig. 8 presents the comparative results obtained by employing the conventional FLC scheme under the same condition. Specifically, the figures display the load voltages (First waveform: \( V_L \)), load currents (Second waveform: \( I_L \)), and phase A load current error (Third waveform: \( i_{eLA} = \hat{i}_{LA} - i_{LA} \)). It is important to note that the load current error waveform in the results of the conventional FLC method is not included because the FLC scheme does not need load current information. It can be observed in Fig. 5 that when the load is suddenly changed, the load output voltage presents little distortion. However, it quickly returns to a steady-state condition in 1.0 ms.
Third: Phase A load current error \( (ieLA = iLA - \hat{i}LA) \).

Fig 9: Simulation results of the proposed observer-based optimal voltage control scheme under nonlinear load with \(-30\%\) parameter variations in \( L_f \) and \( C_f \) (i.e., three-phase diode rectifier)—First: Load output voltages (\( VL \)), Second: Load output currents (\( IL \)), Third: Phase A load current error \( (ieLA = iLA - \hat{i}LA) \).

Fig 10: Simulation results of the conventional FLC scheme under load step change with \(-30\%\) parameter variations in \( L_f \) and \( C_f \) (i.e., balanced resistive load: 0\% – 100\%)—First: Load output voltages (\( VL \)), Second: Load output currents (\( IL \)). (a) Simulation.

Fig 11: Simulation results of the conventional FLC scheme under unbalanced load with \(-30\%\) parameter variations in \( L_f \) and \( C_f \) (i.e., phase B opened)—First: Load output voltages (\( VL \)), Second: Load output currents (\( IL \)).

VIII. CONCLUSION

This paper has proposed a simple observer-based optimal voltage control method of the three-phase UPS systems. The proposed controller is composed of a feedback control term to stabilize the error dynamics of the system and a compensating control term to estimate the system uncertainties. Moreover, the optimal load current observer was used to optimize system cost and reliability. This paper proved the closed-loop stability of an observer-based optimal voltage controller by using the Lyapunov theory. Furthermore, the proposed voltage control law can be methodically designed taking into account a tradeoff between control input magnitude and tracking error unlike previous algorithms. The superior performance of the proposed control system was demonstrated through simulation by implementation of fuzzy controller. Under three load conditions (load step change, unbalanced load, and nonlinear load), the proposed control scheme revealed a better voltage tracking performance such as lower THD, smaller steady-state error, and faster transient response than the conventional FLC scheme even if there exist parameter variations.

REFERENCES


