



Performance Analysis of Wavelet Packet Based SPHIT Algorithm

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Abstract:

The necessity in image compression continuously grows during the last decade. An image compression algorithm based on wavelet packet transform is introduced. This paper introduces an implementation of wavelet packet image compression which is combined with SPIHT (Set Partitioning in Hierarchical Trees) compression scheme. The image compression includes transform of image, quantization and encoding. This paper describes the new approach to construct the best tree on the basis of Huffman coding for further compression.

In this method the tree are known as zero trees and they are efficiently represented by separating the root from the tree to make compression more. Through Experiments (SPIHT Algorithm) we have shown that the image through the wavelet transforms, the wavelet coefficients are generally small value in high frequency region. A large number of experimental results are shown that this method saves a lot of bits in transmission, further enhanced the compression performance.

Key words - Image compression, Wavelet Packet Transforms, Zero trees.

1. Introduction-

Discrete Wavelet Transform (DWT) provides a multiresolution image representation and has become one of the most important tools in image analysis and coding over the last two decades. Image compression algorithms based on DWT provide high coding efficiency for natural (smooth) images. As dyadic DWT does not adapt to the various space-frequency properties of image as, the energy compaction it achieves is generally not optimal [1].

However, the performance can be improved by selecting the transform basis adaptively to the image. Wavelet Packets (WP) represent a generalization of wavelet decomposition scheme. WP image decomposition adaptively selects a transform basis that will be best suited to the particular image.

To achieve that, the criterion for best basis selection is needed.

Coif man and Wickerhauser proposed entropy based algorithm for best basis selection in their work, the best basis is a basis that describes the particular image with the smallest number of basic functions. It is a one-sided metric, which is therefore not optimal in a joint rate-distortion sense. A more practical metric considers the number of bits (rate) needed to approximate an image with a given error (distortion) but this approach and its variation presented can be computationally too intensive. In a fast numerical

Implementation of the best wavelet packet algorithm is provided. Coding results show that fast wavelet packet coder can significantly outperform a sophisticated wavelet coder constrained to using only a dyadic decomposition, with a negligible increase in computational load.

The goal of this paper is to demonstrate advantages and disadvantages of using WP decomposition in SPIHT-based codec. SPIHT algorithm was introduced by Said and Pearlman, and is improved and extended version of Embedded Zero tree Wavelet (EZW) coding algorithm Both algorithms work with tree structure, called Spatial Orientation Tree (SOT), that defines the spatial relationships among wavelet coefficients in different decomposition sub bands. In this way, an efficient prediction of significance of co efficient based on significance of their "parent" coefficients is enabled. The main contribution of Shapiro's work is zero tree quantization of waveletCoefficients and introduction of special zero tree symbol indicating that all coefficients in a SOT are found to be insignificant with respect to a particular quantization threshold. An embedded zero trees quantize refines each input coefficient sequentially using a bitplane coding scheme, and it stops when the size of the encoded bit stream reaches the target bit-rate. SPIHT coder provides gain in PSNR over EZW due to introduction of a special symbol that indicates significance of child nodes of a significant parent and separation of child

nodes (direct descendants) from second-generation descendants.

To date, there have been numerous variants and extensions to SPIHT algorithm, for example: 3-D SPIHT for video coding, SPIHT for color image coding, and scalable SPIHT for network applications.

Since the SPIHT algorithm relies on Spatial Orientation Trees (SOT) defined on dyadic sub band structure, there are a few problems that arise from their adaptation to WP decomposition. First is the so-called parental conflict that happens when in the wavelet packet tree one or more of the child nodes are at the coarser scale than the parent node. It must be resolved in order that SOT structure with well-defined parent-child relationships for arbitrary wavelet decomposition can be created. Xiong et al. avoided the parental conflict by restricting the choice of the basis. In their work the Space-Frequency Quantization (SFQ) algorithm is used. SFQ algorithm employs a rate-distortion (R-D) optimization framework for selecting the best basis and to assign an optimal quantize to each of the wavelet packet sub bands. Wavelet packet geometry and offered a general structure for an arbitrary WP decomposition. In their work a Compatible Zero tree Quantization (CZQ) is utilized,

2. SET PARTITIONING IN HIERARCHICAL TREES (SPIHT) ALGORITHM

Image Codec Based on SPIHT

Set Partitioning in Hierarchical Trees (SPIHT) is an image compression algorithm that exploits the inherent similarities across subbands in a wavelet decomposition of an image. It implies uniform quantization and bit allocation applied after wavelet decomposition.

General description:

The algorithm codes the most important (in the sense of MSE reduction) wavelet transform coefficients in priority, and transmits the bits so that an increasingly refined copy of the original image is obtained with time.

The SPIHT is considered the premier state-of-the-art algorithm in image compression, and has excellent coding performance for 1-D signals. This algorithm has been modified gradually; some of its modified versions: ESPIHT, MSPIHT and etc.

The order in which coefficients are transmitted is recovered on the decoder using information of comparisons and sets being examined

for significance during the sort, sets are created using hierarchical tree structure, i.e. Set Partition in Hierarchical Trees.

One of the advantages with SPIHT is that it produces an (optimal) embedded bitstream. This means that the bitstream can be truncated at any instant, and is then guaranteed to yield the best possible reconstruction.

Compression Algorithm:

A PostScript version of the paper describing SPIHT is available via [anonymous ftp](#). Here we take the opportunity to comment how it is different from other approaches.

SPIHT represents a small "revolution" in image compression because it broke the trend to more complex (in both the theoretical and the computational senses) compression schemes. While researchers had been trying to improve previous schemes for image coding using very sophisticated vector quantization, SPIHT achieved superior results using the simplest method: uniform scalar quantization. Thus, it is much easier to design fast SPIHT codecs.

Actually, we do expect better compression results from vector quantizers in the future (someday, somewhere, as prophesied by Shannon), but it is unknown if their speed will justify the gains.

SPIHT algorithm

In the SPIHT algorithm, the image is first decomposed into a number of subbands by means of hierarchical wavelet decomposition. The subband coefficients are then grouped into sets known as spatial-orientation trees, which efficiently exploit the correlation between the frequency bands. The coefficients in each spatial orientation tree are then progressively coded from the most significant bit-planes (MSB) to the least significant bit-planes (LSB), starting with the coefficients with the highest magnitude and at the lowest pyramid levels. The SPIHT multistage encoding process employs three lists and sets:

- SPIHT has 3 lists
 - LIP: list of insignificant pixels (individual insignificant coefficients)
 - LIS: list of insignificant lists (insignificant trees)
 - LSP: list of significant pixels (significant coefficients)
- SPIHT defines 2 types of trees

- Type D: check all descendants for significance
- Type L: check all descendants except immediate children
- Other features
 - Root node is checked independently of the rest of the tree
 - SPIHT sorting pass checks significance of LIP & LIS elements, then moves significant coefficients to LSP

SPIHT Basic Algorithm

Step 1: Initialization

Compute initial threshold

LIP: all root nodes (in lowpass subband)

LIS: all trees (type D)

LSP: empty

Step 2: Sorting Pass

Check significance of all coefficients in LIP :

If significant, output 1 followed by a sign bit & move it to LSP.

If insignificant, output 0.

Step 3: Check significance of all trees in LIS For type-D tree :

If significant, output 1 & proceed to code its children

If a child is significant, output 1, sign bit, & add it to LSP.

If a child is insignificant, output 0 and add it to the end of LIP.

If the child has descendants, move the tree to the end of LIS as type L, otherwise remove it from LIS.

If insignificant, output 0.

For type-L tree :

If significant, output 1, add each of the children to the end of LIS as type D and remove the parent tree from LIS.

If insignificant, output 0.

Step 4: Refinement pass

For each element in LSP – except those just added above, output the nth most significant bit of coefficient.

End loop over LSP.

Step 5: Decrease the threshold by a factor of 2. Go to Step 2.

3. PROPOSED WAVELET PACKETS TREE

A. Wavelet Packets

The wavelet packet method is a generalization of wavelet decomposition that offers a richer signal analysis. Wavelet packet atoms are waveforms indexed by three naturally interpreted parameters i.e. position, scale (as in

wavelet decomposition), and frequency. For a given orthogonal wavelet function, we generate a library of bases called wavelet packet bases. Each of these bases offers a particular way of coding signals, preserving global energy, and reconstructing exact features. The wavelet packets can be used for numerous expansions of a given signal.

Zerotree quantization is an effective way of exploiting the self-similarities among high frequency subbands at various resolutions. The main thrust of this quantization strategy is in the prediction of the significance of corresponding wavelet coefficients in higher frequency sub bands at the finer resolutions by exploiting the parent-offspring relationship. This prediction works well, in terms of efficiently encoding the wavelet coefficients, due to the statistical characteristics of sub bands at various resolutions and is related to the scale-invariance of edges in high frequency sub bands of similar orientation. Moreover, embedded (progressive) transmission and reconstruction, which is required in some applications, using zero trees with successive approximation quantization (SAQ), is quite straightforward.

B. Wavelets to wavelet packets decomposing.

The orthogonal wavelet decomposition procedure splits the approximation coefficients into two parts. After splitting we obtain a vector of approximation coefficients and a vector of detail coefficients both at a coarser scale. The information lost between two successive approximations is captured in the detail coefficients. Then the new approximation coefficient vector is split again. In the wavelet packet approach, each detail coefficient vector also decomposed into two parts as in approximation vector splitting.

C. Building Wavelet Packets

The computation scheme for wavelet packets generation is easy when using an orthogonal wavelet. We start with the two filters of length 2N.

$$W_n(x), \quad n=0,1,2,3)$$

$$w_{2n}(x) = \sqrt{2} \sum_{k=0}^{2N-1} h(k) \cdot w_n(2x - k)$$

$$w_{2n+1}(x) = \sqrt{2} \sum_{k=0}^{2N-1} g(k) \cdot w_n(2x - k)$$

h(n) and g(n), corresponding to the

wavelet. $W_0(x) = \Phi(x)$ is the scaling function and $W_1(x) = \Psi(x)$ is the wavelet function. An idea of wavelet packet is the same as wavelet. Only difference is that wavelet packet offers a more complex and flexible analysis. In wavelet packet analysis the details as well as the approximation are split. The wavelet packet tree for 3-level decomposition is shown in Figure 2.

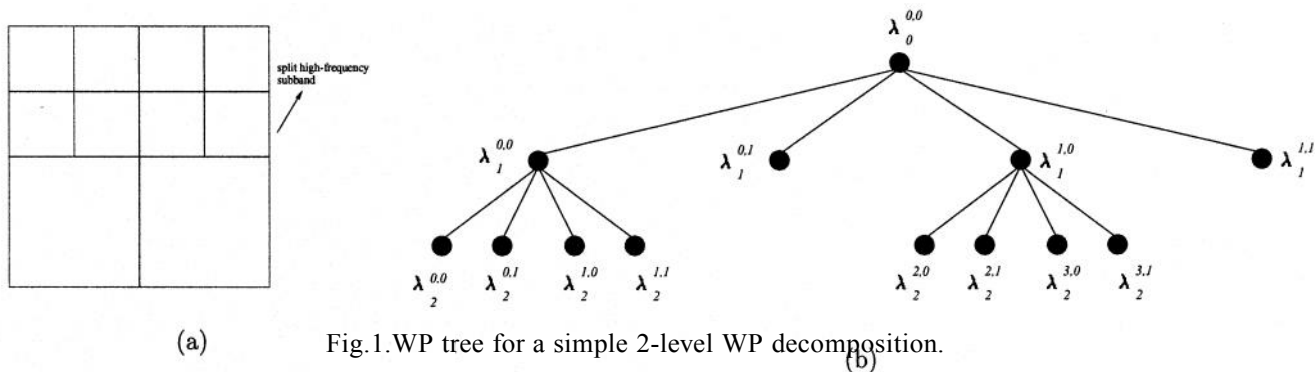


Fig.1.WP tree for a simple 2-level WP decomposition.

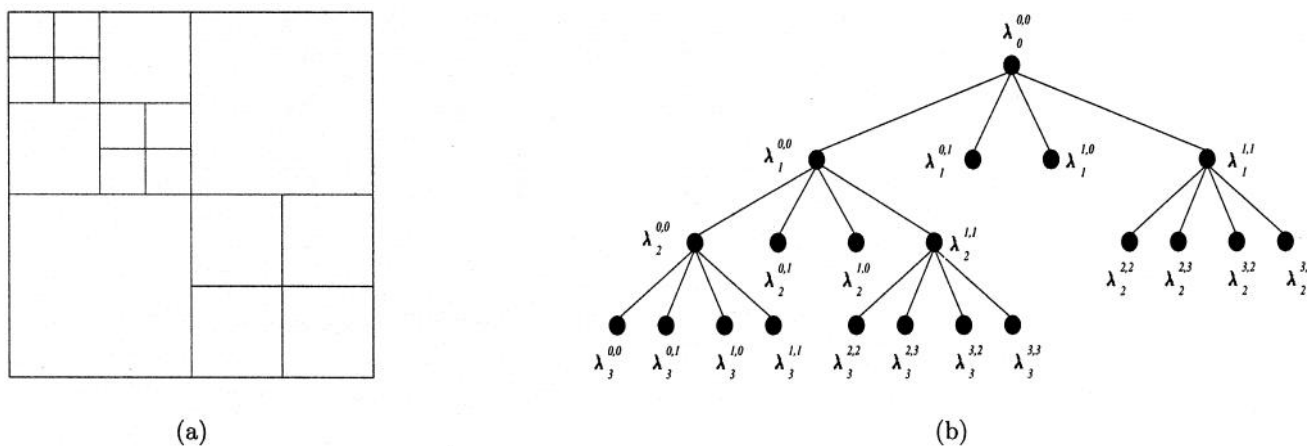


Fig.2.WP tree for a 3-level WP decomposition.

In this paper Shannon entropy criteria is used to construct the best tree. Shannon entropy criteria find the information content of signal 'S'.

$$\text{Entropy}(S) = \sum_i S_i^2 \log S_i^2 \quad (2)$$

The value of threshold is calculated based on

nature of image and type of wavelet used for decomposition.

$$\text{Threshold} = K - \text{Sqrt}(\text{mean}(w_energy(T) \times 100))$$

D. The Proposed Algorithm

The algorithm is described as follows:

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IEEE TRANSACTIONS ON IMAGE
PROCESSING, VOL. 21, NO. 1, JANUARY 2012